

Electron Kinetic Processes in the Solar Wind

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Kinetic properties of corona and wind

- **Plasma is multi-component and non-uniform**

- multiple scales and complexity

- **Plasma is tenuous and turbulent**

- free energy for microinstabilities

- strong wave-particle interactions (diffusion)

- weak collisions (Fokker-Planck operator)

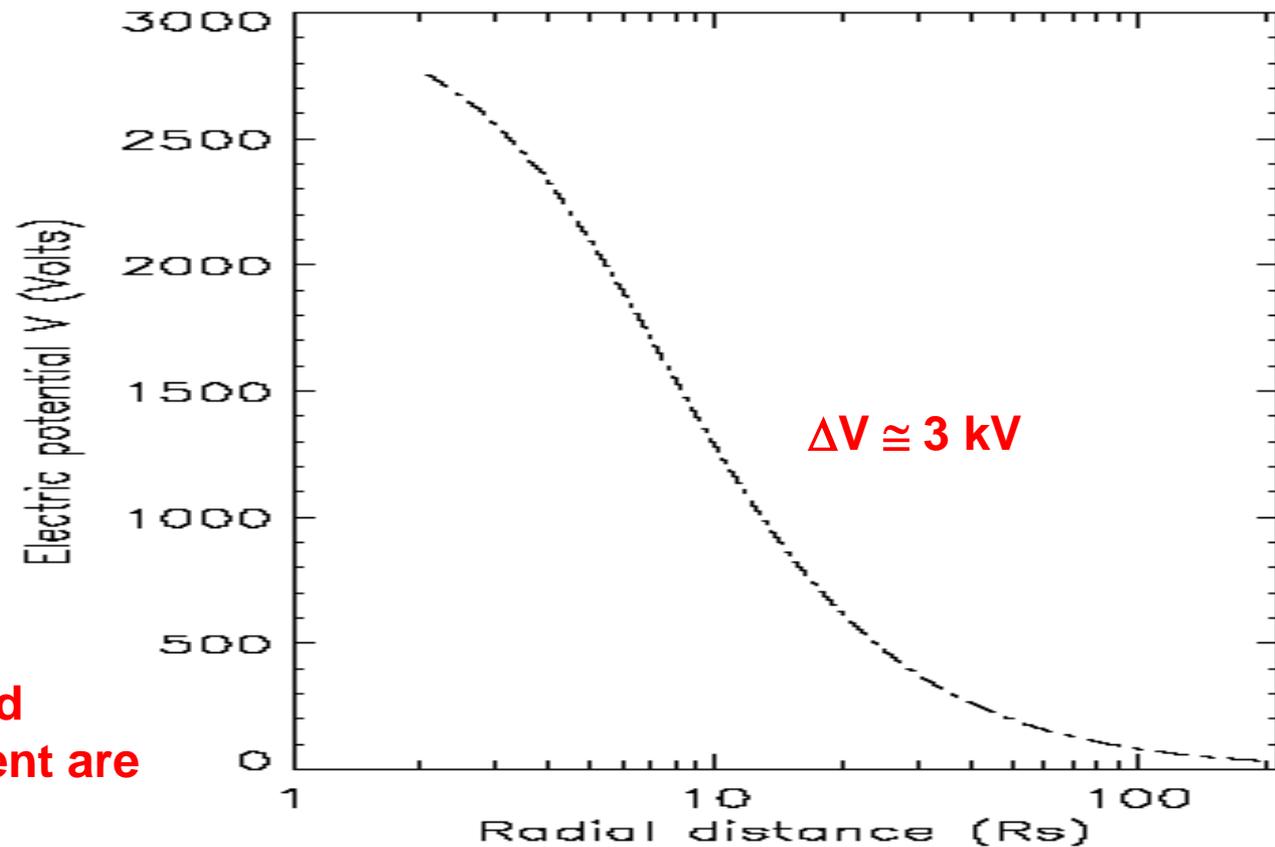
- strong deviations from local thermal equilibrium

- global boundaries are reflected locally

- suprathermal particles

Problem: Thermodynamics and transport....

Collisional fluid versus exosphere



Total energy and magnetic moment are conserved:

$$E = \frac{m}{2}(v_{\perp}^2 + v_{\parallel}^2) - \frac{m}{2}\Omega_{\odot}^2 r^2 \cos^2 \lambda + m\Phi_g(r) + q\Phi_e(r), \quad \mu = \frac{mv_{\perp}^2}{2B(r)}$$

Kinetic Vlasov-Boltzmann theory

Description of particle velocity distribution function in phase space:

$$\frac{df}{dt} + \mathbf{w} \cdot \frac{\partial f}{\partial \mathbf{x}} + (\mathbf{w} \times \boldsymbol{\Omega}) \cdot \frac{\partial f}{\partial \mathbf{w}} + \left(-\frac{d}{dt} \mathbf{u} + \frac{q}{m} \mathbf{E}'\right) \cdot \frac{\partial f}{\partial \mathbf{w}} - \frac{\partial \mathbf{u}}{\partial \mathbf{x}} : \mathbf{w} \frac{\partial f}{\partial \mathbf{w}} = \frac{\delta f}{\delta t}$$

Convective derivative:

$$\frac{d}{dt} = \frac{\partial}{\partial t} + \mathbf{u} \cdot \frac{\partial}{\partial \mathbf{x}}$$

Relative velocity \mathbf{w} ,
mean velocity $\mathbf{u}(\mathbf{x}, t)$,
gyrofrequency $\boldsymbol{\Omega}$, electric
field \mathbf{E}' in moving frame:

$$\mathbf{w} = \mathbf{v} - \mathbf{u}(\mathbf{x}, t), \quad \boldsymbol{\Omega} = \frac{q\mathbf{B}}{mc}, \quad \mathbf{E}' = \mathbf{E} + \frac{1}{c} \mathbf{u} \times \mathbf{B}$$

Moments: Drift
velocity, pressure
(stress) tensor,
heat flux vector

$$\langle \mathbf{w} \rangle = 0, \quad \mathcal{P} = nm \langle \mathbf{w} \mathbf{w} \rangle, \quad \mathbf{Q} = nm \langle \mathbf{w} \frac{1}{2} w^2 \rangle$$

$$\boldsymbol{\Pi} = \mathcal{P} - \mathcal{I}p \quad p = nk_B T = \frac{1}{3} \text{Tr} \mathcal{P}$$

Dum, 1990

Collisions and plasma turbulence

Coulomb collisions and wave-particle interactions can be represented by a second-order differential operator, including the acceleration vector $\mathbf{A}(\mathbf{v})$ and diffusion tensor $\mathcal{D}(\mathbf{v})$, in velocity space:

$$\frac{\delta f}{\delta t} = \frac{\partial}{\partial \mathbf{v}} \cdot \left(-\mathbf{A} + \mathcal{D} \cdot \frac{\partial}{\partial \mathbf{v}} \right) f$$

Parameter	Chromo-sphere	Corona (1R _s)	Solar wind (1AU)
n_e (cm ⁻³)	10 ¹⁰	10 ⁷	10
T_e (K)	6-10 10 ³	1-2 10 ⁶	10 ⁵
λ_e (km)	10	1000	10 ⁷

Collisional kinetics of solar wind electrons:

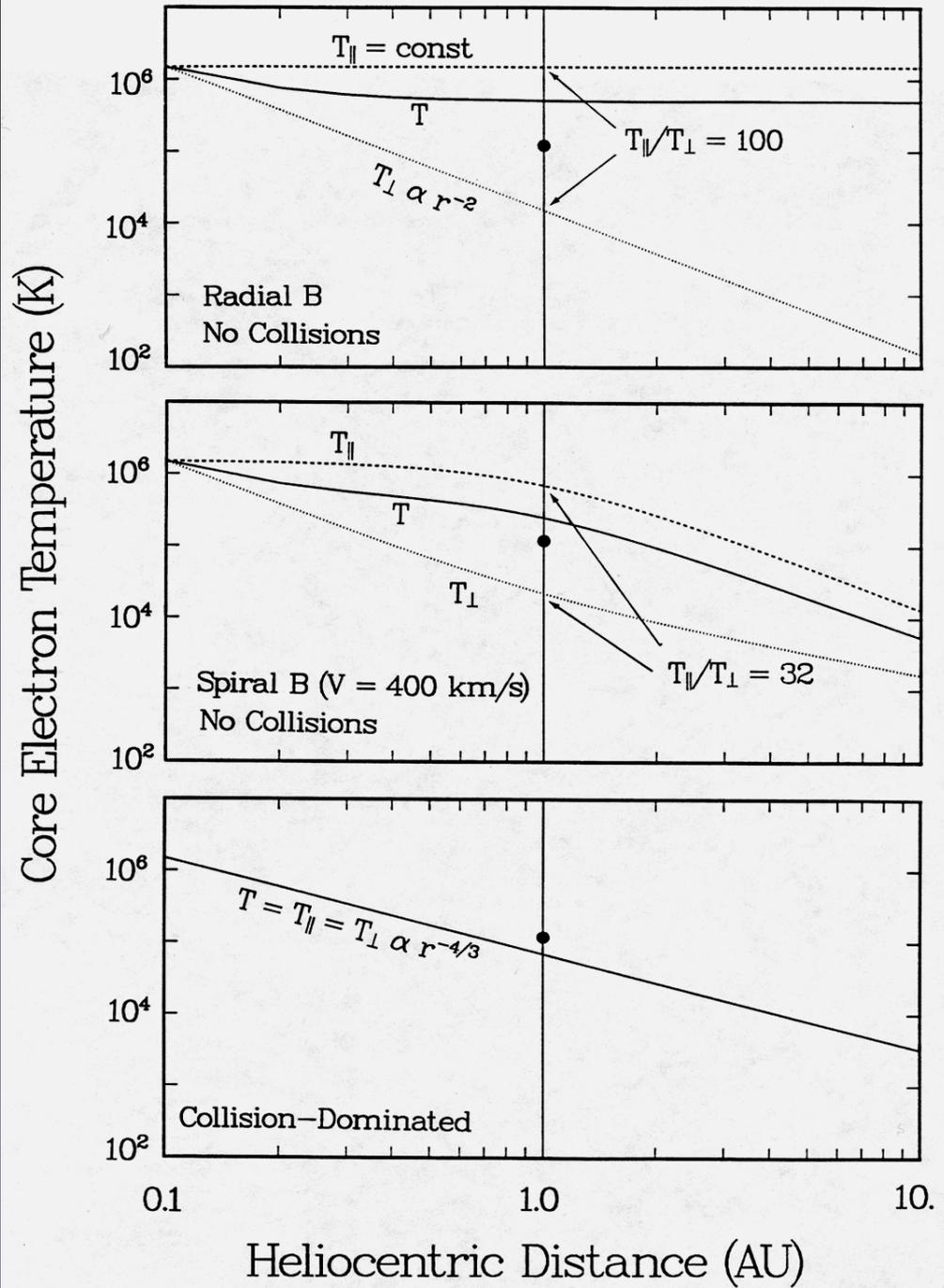
- Pierrard et al.
- Lie-Svendensen et al.

Collisions and geometry

Double adiabatic invariance,
→ extreme anisotropy is not observed!

Spiral reduces anisotropy!

Adiabatic collision-dominated
→ isotropy, is not observed!



Plasma waves and frequencies

- **Electrostatic** (Debye length, $\lambda_{Dj} \sim 2\pi/k_j \sim 1\text{ m}$)
 - Langmuir and ion-acoustic: $\omega_j = k_j V_j$; $V_j = (k_B T_j / m_j)^{1/2}$
- **Electromagnetic** (Gyroradius, $r_j \sim V_j / \Omega_j \sim 100\text{ km}$)
 - Whistler and lower-hybrid: $\Omega_e, (\Omega_e \Omega_i)^{1/2}$
 - Alfvén and ion-cyclotron: Ω_p, Ω_α ; $\Omega_i = e_i B / m_i c$
 - Fast-mode and magneto-acoustic: $\Omega_j = k_{Aj} V_A$

Inside 1 AU these frequencies range from 10 Hz up to 100 MHz.

- **Gyrokinetic scale:** $\Omega_j = K_j V_{sw}$; at boundaries and ion pick-up
- **Doppler shift:** $\omega' = \omega + k V_{sw}$; in supersonic wind

Solar Orbiter will measure the full electromagnetic (vector) fields and their fluctuations.

Electron energy spectrum

IMP spacecraft

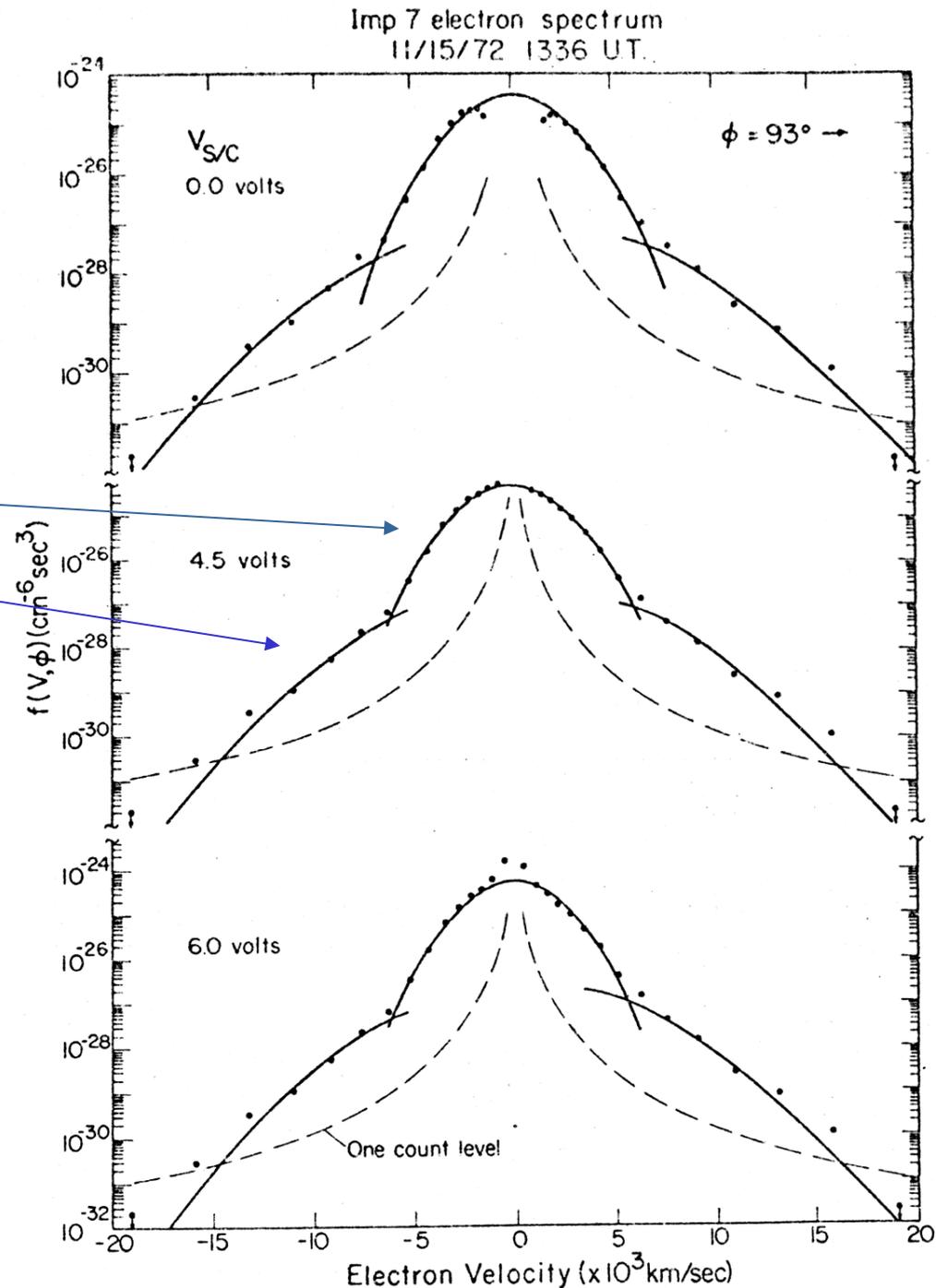
Two populations:

- Core (96%)
- Halo (4%)

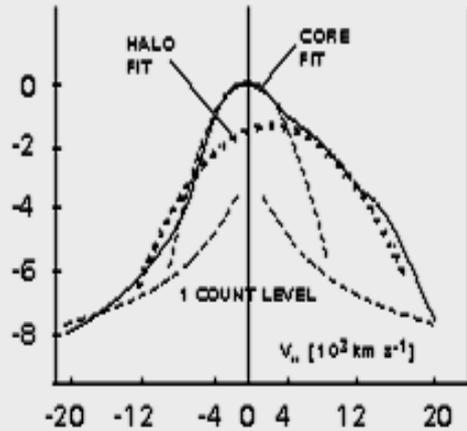
Core: local, collisional, **bound** by interplanetary electrostatic potential

Halo: global, collisionless, **free** to escape (exospheric)

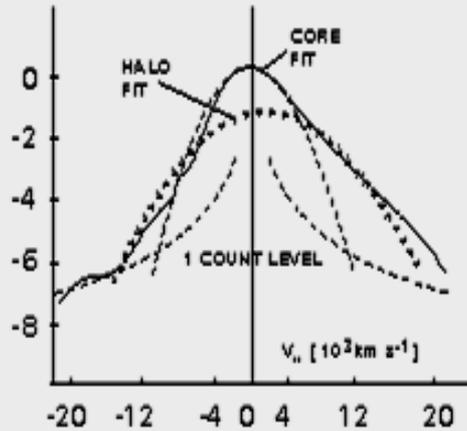
Feldman et al., JGR, 80, 4181, 1975



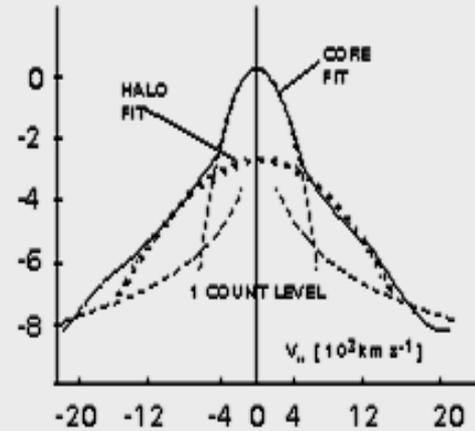
Electron velocity distributions



high

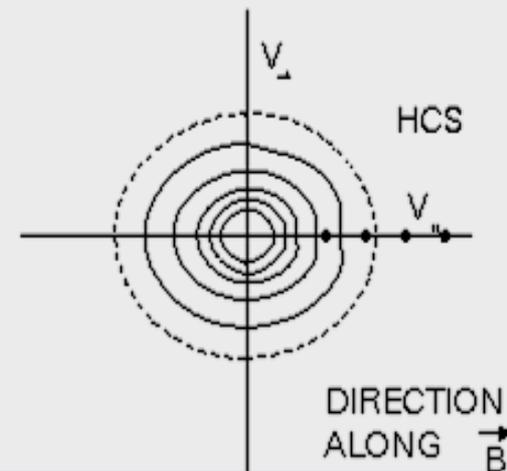
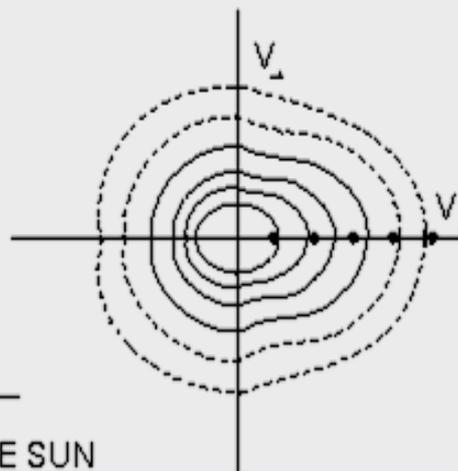
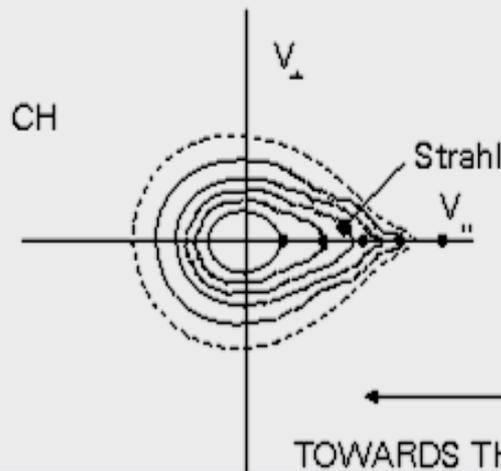


intermediate speed



low

$T_e = 1-2 \times 10^5 \text{ K}$



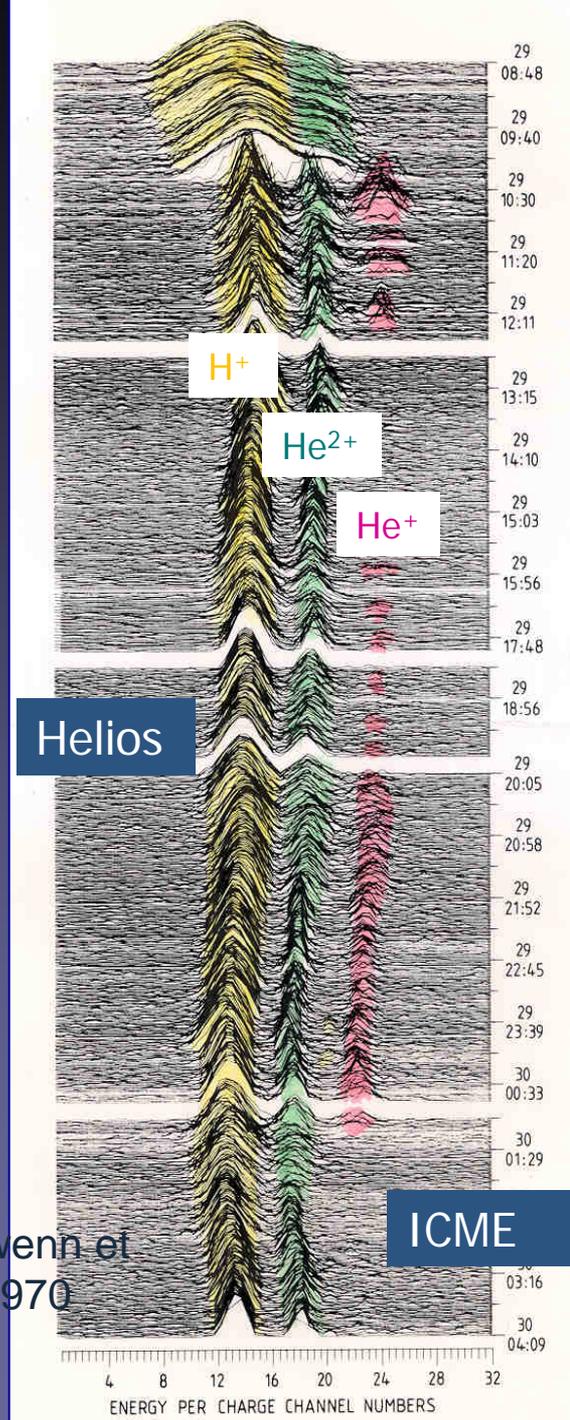
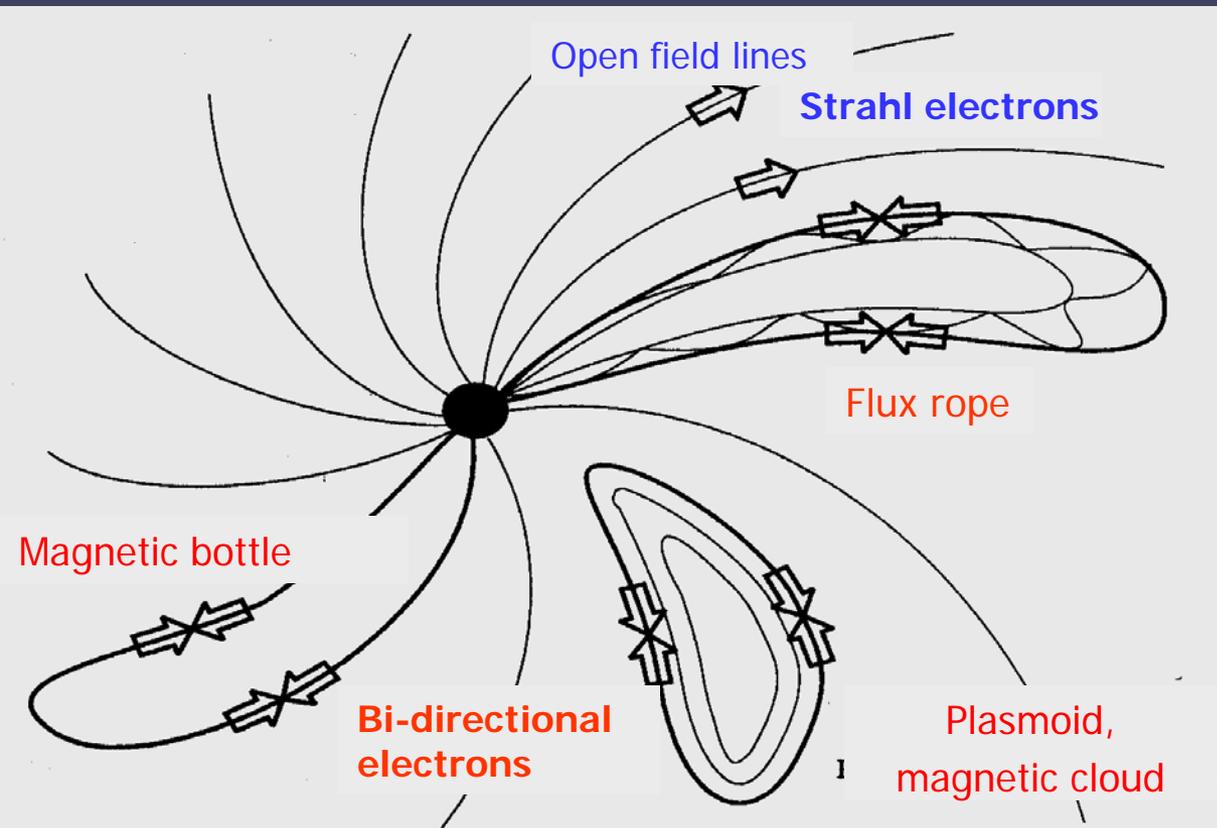
Helios

Pilipp et al., JGR, 92, 1075, 1987

Core (96%), halo (4%) electrons, and „strahl“

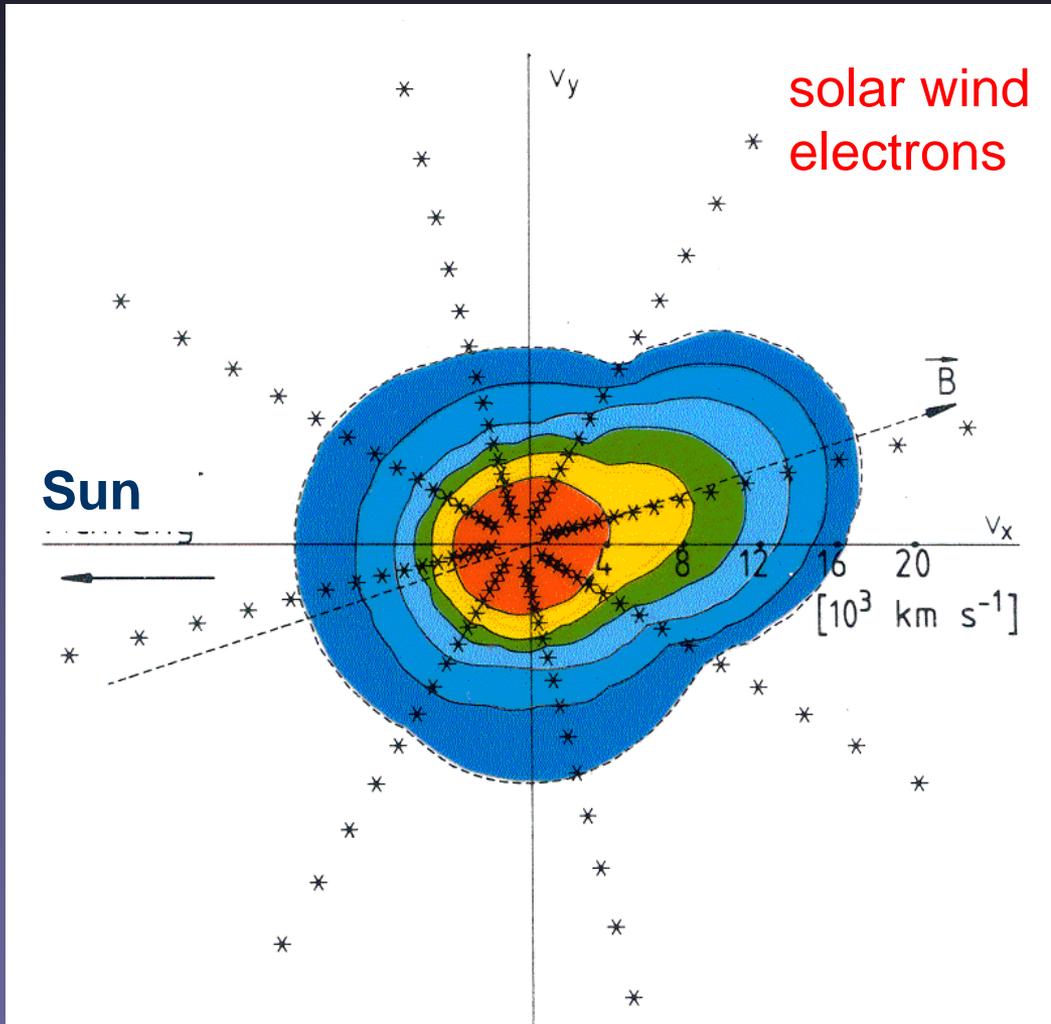
Bi-directional electron heatfluxes and rare He⁺

- Palmer et al., 1978, Solar energetic electrons indicate bottle
- Kutchko et al., 1982, Bi-dir. ions and trapped electrons in loop
- Pillipp et al., 1987, Double-strahl solar-wind electrons in loop
- Gosling et al., 1987, Bi-dir. suprathermal electrons in cloud



Schwenn et al., 1970

Invalidity of classical transport theory



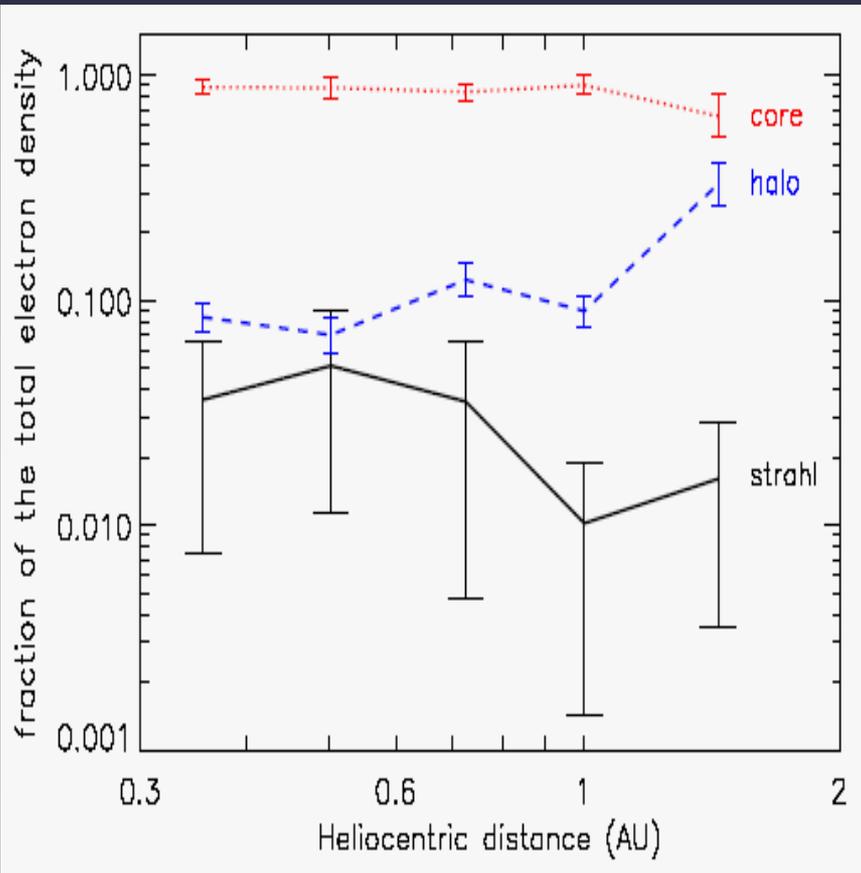
$$n_e = 3-10 \text{ cm}^{-3},$$

$$T_e = 1-2 \cdot 10^5 \text{ K at 1 AU}$$

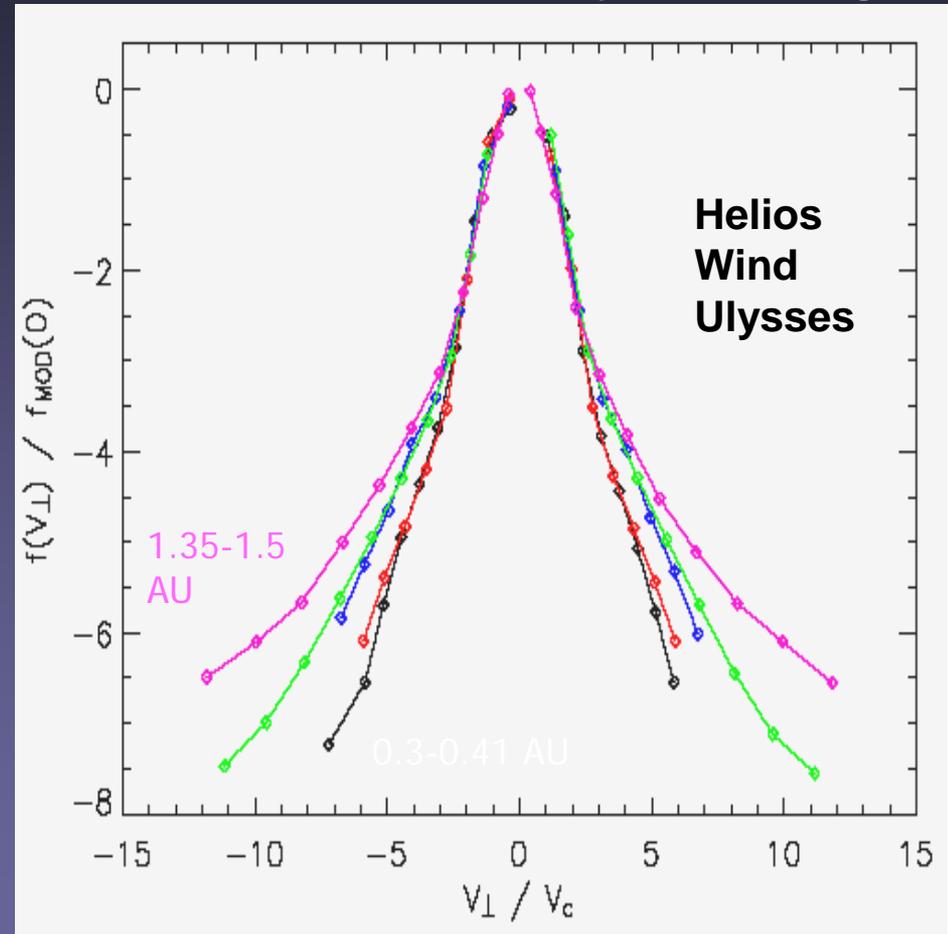
- Strong heat flux tail: Strahl
- Collisional free path λ_c much larger than temperature-gradient scale L
- Polynomial expansion about a local Maxwellian hardly converges, as $\lambda_c \gg L$

Solar wind electrons: Core-halo evolution

Halo is relatively increasing while strahl is diminishing.



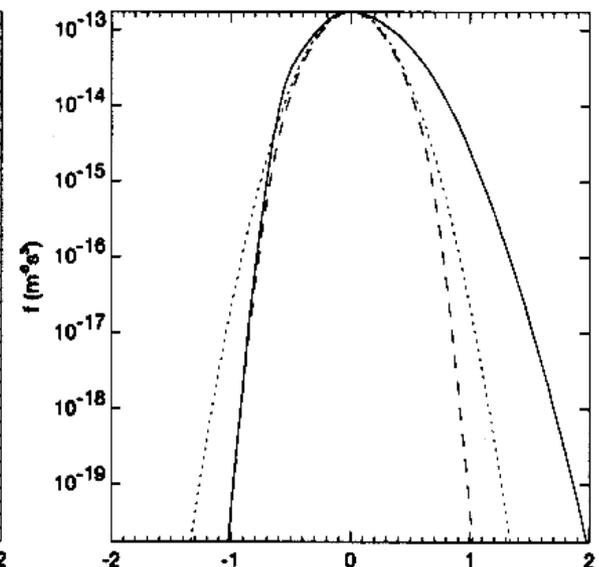
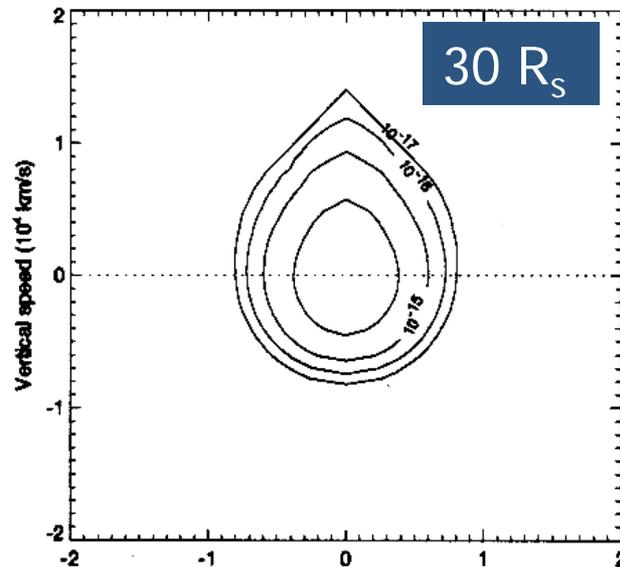
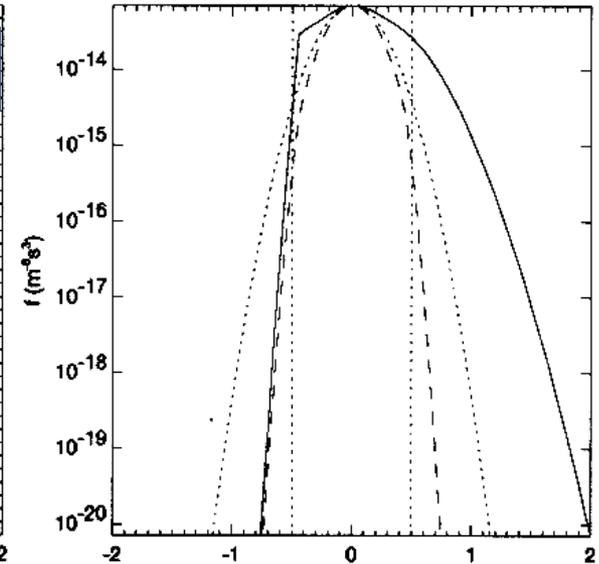
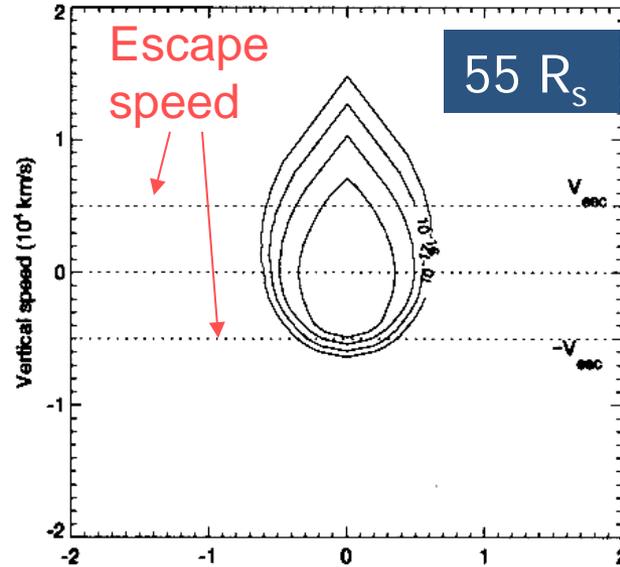
Normalized core remains constant while halo is relatively increasing.



Coulomb collisions and electrons

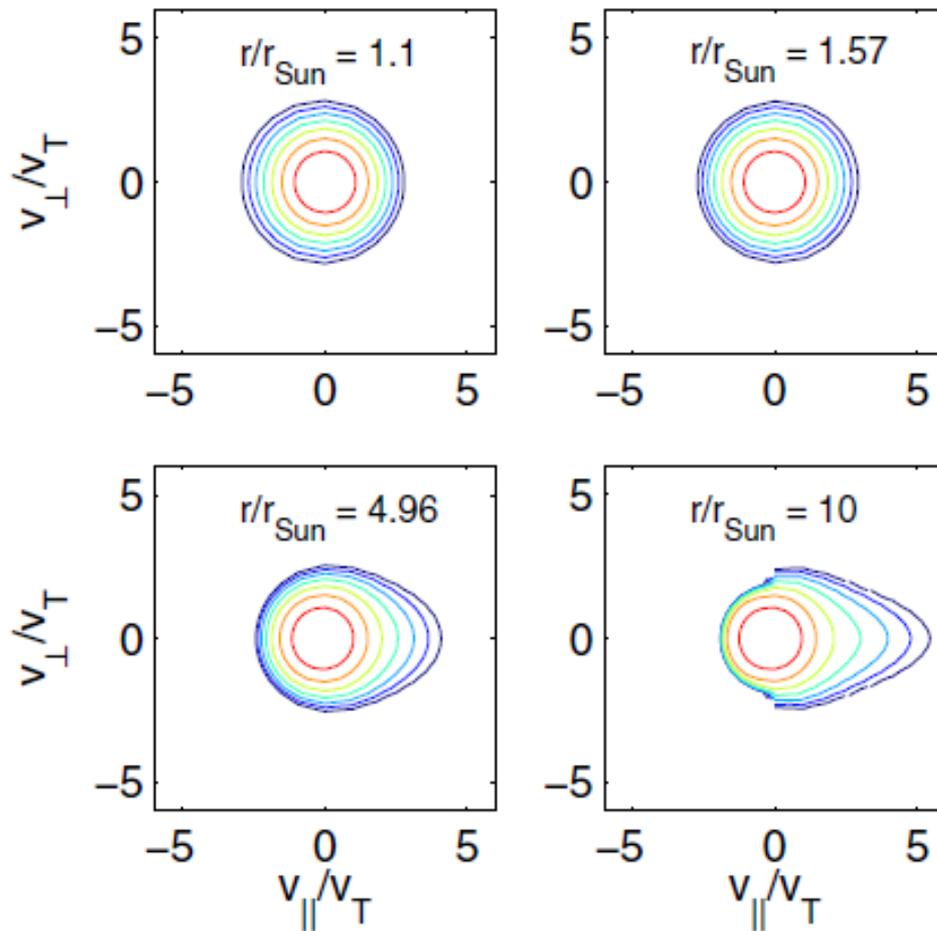
Integration of the full Fokker-Planck equation

- Velocity filtration is weak
- Strahl formation by escape electrons
- Core bound by electric field

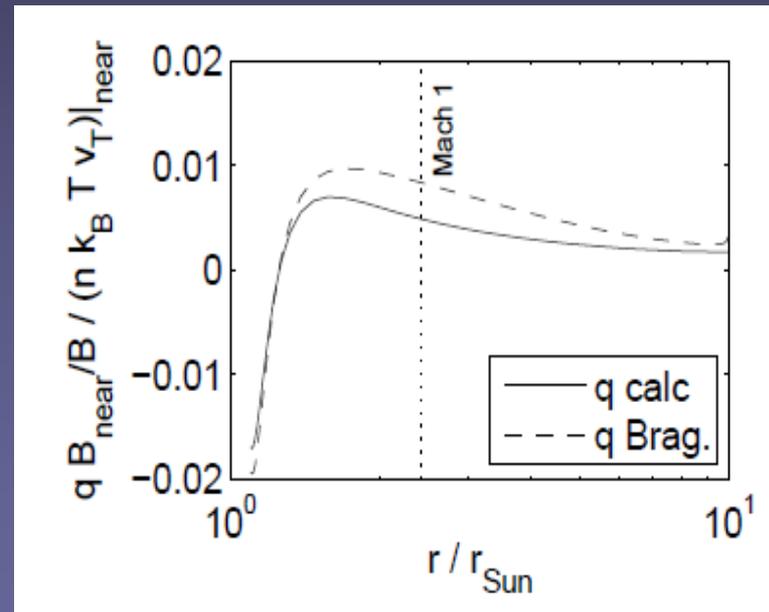


Lie-Svendson et al.,
JGR, **102**, 4701, 1997

Collisional core – runaway strahl



Collisional transport in corona with Fokker-Planck operator in Boltzmann equation with self-consistent electric field



Wave-particle interactions

Dispersion relation using measured or model **distribution functions** $f(\underline{v})$, e.g. for electrostatic waves:

$$\varepsilon_L(\underline{k}, \omega) = 0 \rightarrow \omega(\underline{k}) = \omega_r(\underline{k}) + i\gamma(\underline{k})$$

Dielectric constant is functional of $f(\underline{v})$, which may when being non-Maxwellian contain free energy for wave excitation.

$\gamma(\underline{k}) > 0 \rightarrow$ **micro-instability.....**

Resonant particles:

$$\omega(\underline{k}) - \underline{k} \cdot \underline{v} = 0 \quad (\text{Landau resonance})$$

$$\omega(\underline{k}) - \underline{k} \cdot \underline{v} = \pm \Omega_j \quad (\text{cyclotron resonance})$$

\rightarrow Energy and momentum exchange between waves and particles. Quasi-linear or non-linear relaxation.....

Electron heat conduction

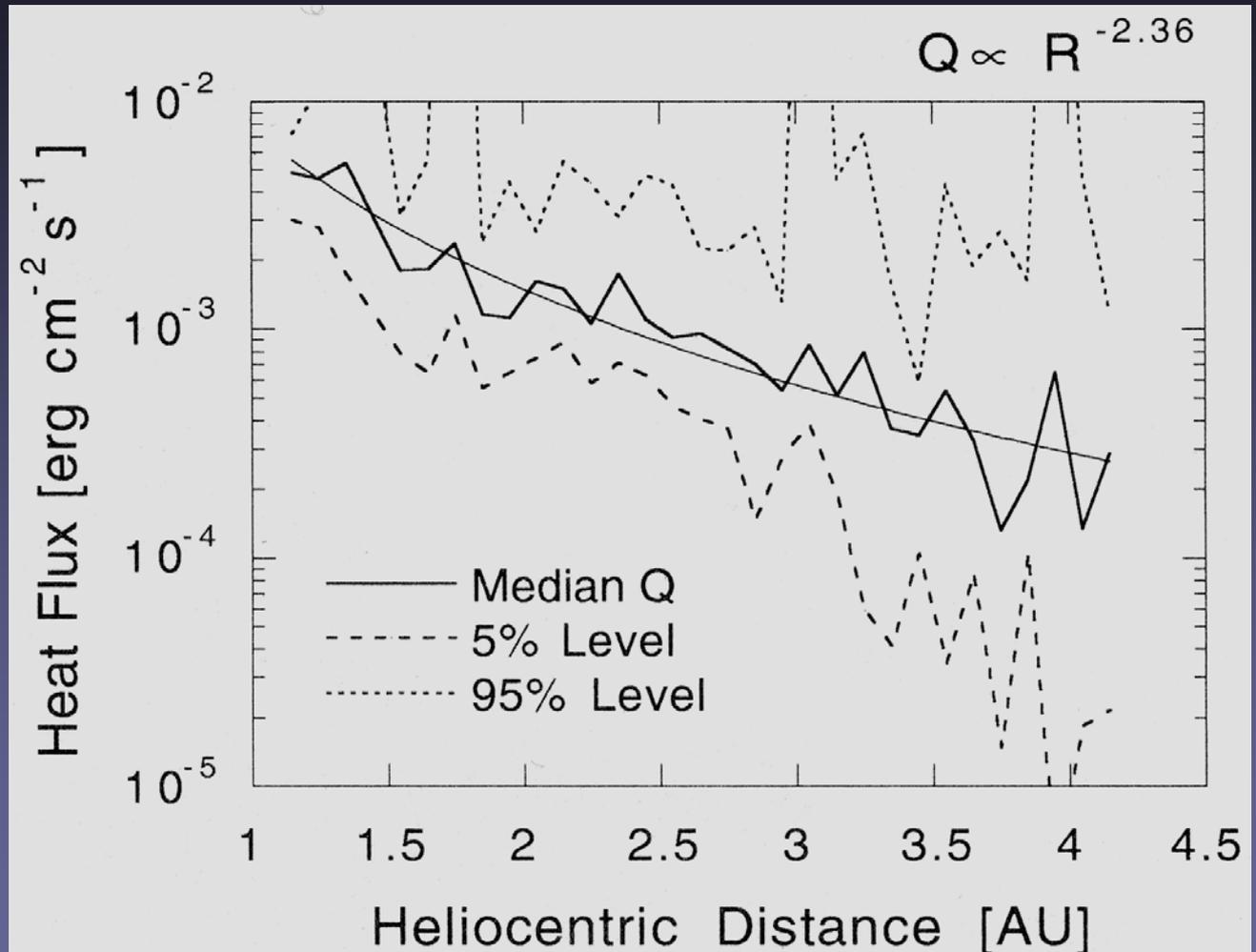
Heat carried by
halo electrons!

$$T_H = 7 T_C$$

Interplanetary
potential:

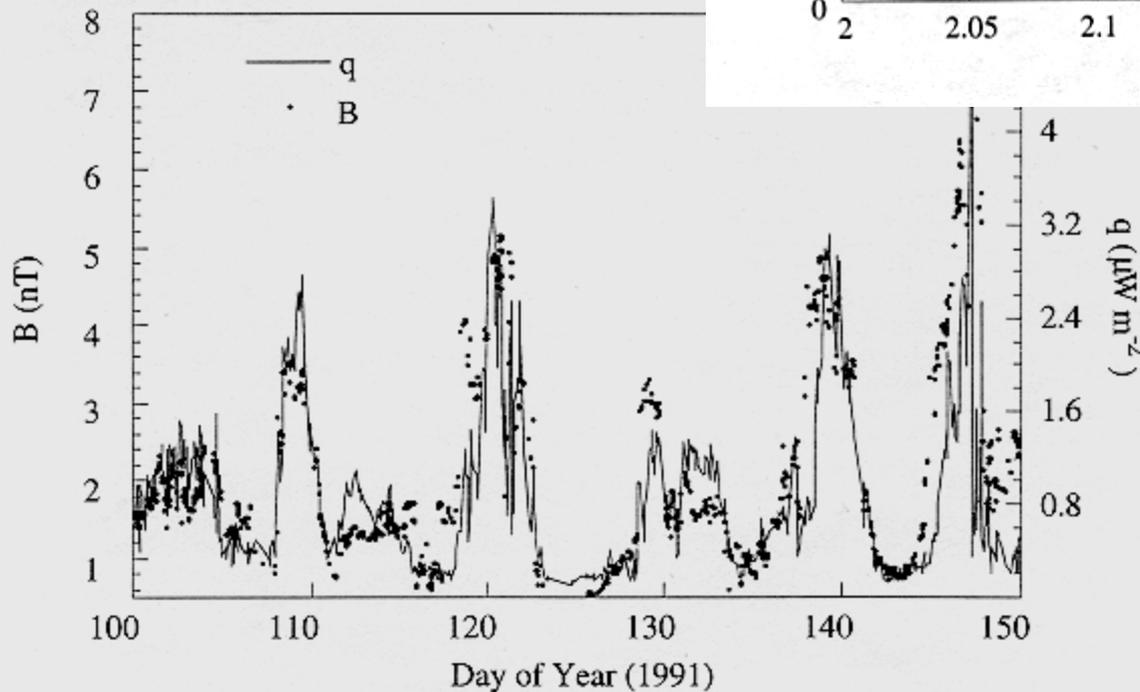
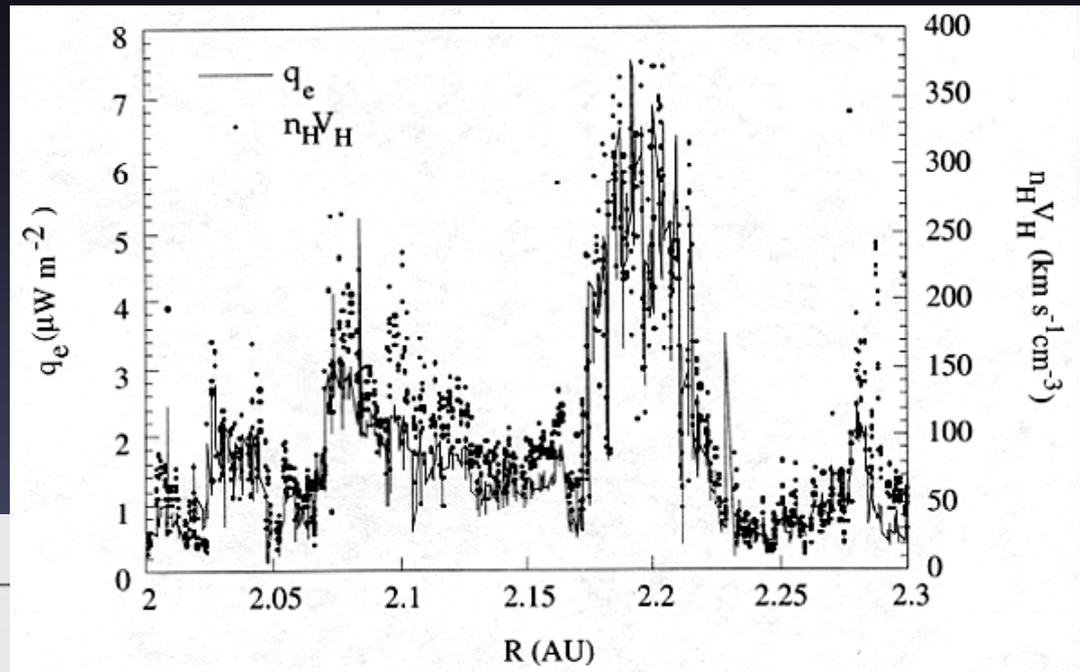
$$\Phi = 50\text{-}100 \text{ eV}$$

$$\underline{E} = -1/n_e \underline{\nabla} p_e$$



$$\underline{Q}_e \neq -\kappa \underline{\nabla} T_e$$

Whistler regulation of electron heat flux



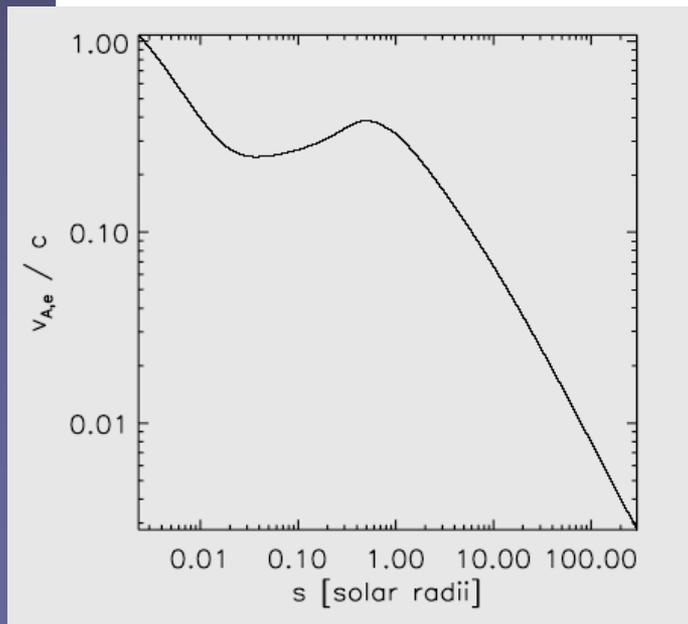
- Halo electrons carry heat flux
- Heat flux varies with B or V_A
- Whistler instability regulates drift

Suprathermal coronal electrons caused by wave-particle interactions I

$$\frac{\partial f}{\partial t} + v_{\parallel} \frac{\partial f}{\partial s} + \left(g_{\parallel} - \frac{e}{m_e} E_{\parallel} \right) \frac{\partial f}{\partial v_{\parallel}} + \frac{v_{\perp}}{2A} \frac{\partial A}{\partial s} \left(v_{\perp} \frac{\partial f}{\partial v_{\parallel}} - v_{\parallel} \frac{\partial f}{\partial v_{\perp}} \right) = \left(\frac{\delta f}{\delta t} \right)_{w-p} + \left(\frac{\delta f}{\delta t} \right)_{\text{Coul}} \quad (7)$$

Boltzmann equation with waves and collisions

A(s) flux tube area function

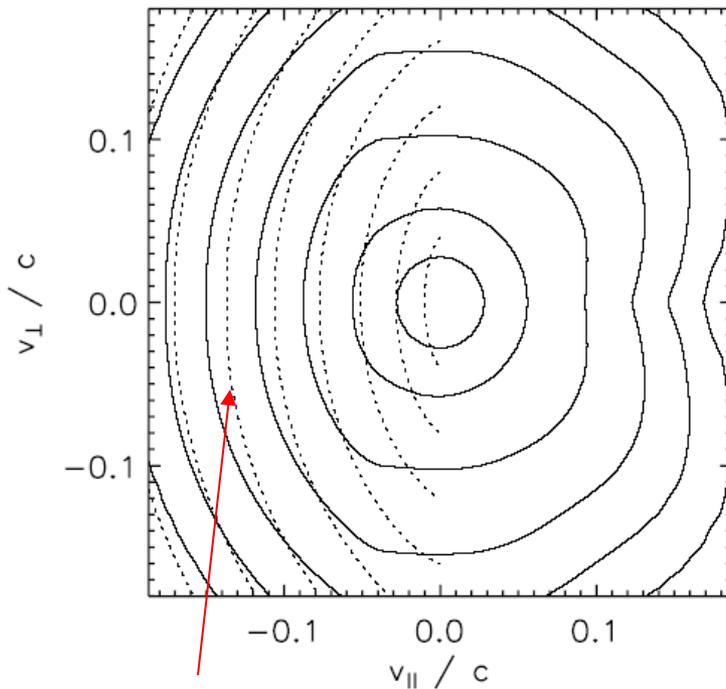


Electron pitch-angle scattering in the whistler wave field

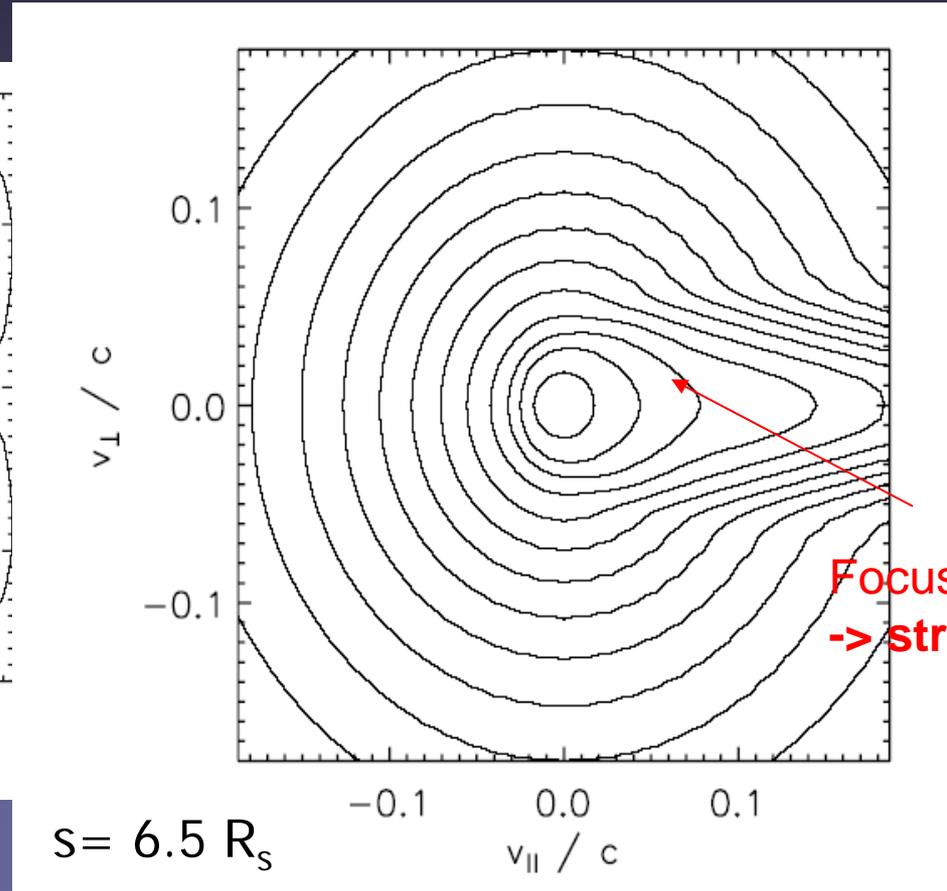
Normalized phase speed $v_{A,e}/c$ in the solar corona

Suprathermal coronal electrons caused by wave-particle interactions II

$s = 0.014 R_s$



Pitch-angle scattering
-> shell formation



$s = 6.5 R_s$

Conclusions

- Solar wind electron velocity distributions are shaped generally by large-scale forces (e.g., gravity, magnetic mirror force), Coulomb collisions and resonant interactions with high-frequency plasma waves.
- The core electrons are formed mainly by gravity and the interplanetary potential and isotropised by Coulomb collisions.
- The strahl electrons are free (they can climb the interplanetary potential) collisional run-away particles that strongly focus along the magnetic field.
- Collisional transport is non-classical and less effective than transport according to Braginskii's theory.
- Diffusion implies inelastic scattering of electrons by ion acoustic and whistler mode waves, and thus leads to turbulence dissipation at the electron kinetic scales.